

I B.Tech Regular Examinations, June 2010**MATHEMATICS-1**

**Common to ME, CHEM, BME, IT, MECT, MEP, AE, BT, AME, ICE,
E.COMP.E, MMT, ETM, EIE, CSE, ECE, EEE, CE**

Time: 3 hours**Max Marks: 75**

**Answer any FIVE Questions
All Questions carry equal marks**

1. (a) Find the radius of curvature at any point on $y^2 = 4ax$ and hence show that the radius of curvature at the vertex is equal to the semi latus rectum.
(b) Trace the curve $r = a(1 + \cos \theta)$ [7+8]
2. (a) Find the volume of Spherical cap of height h cut off from a sphere of radius a.
(b) Evaluate $\int_0^\pi \int_0^{a(1+\cos \theta)} r^2 \cos \theta dr d\theta$ [8+7]
3. (a) Solve the differential equation $(D^2 + D + 1)y = x^3$
(b) Solve the differential equation $(D^2 + 1)y = \sin x \sin 2x$ [8+7]
4. (a) Form the differential equation by eliminating arbitrary constants
 $y = a x^3 + b x^2$
(b) Solve the differential equation $x^3 \frac{dy}{dx} = y^3 + y^2 \sqrt{y^2 - x^2}$
(c) Find the orthogonal Trajectories of the family of curves $x^2 + y^2 = a^2$ [4+6+5]
5. (a) If $u = x^2 - 2y, v = x + y + z, w = x - 2y + 3z$ find $\frac{\partial(u,v,w)}{\partial(x,y,z)}$
(b) Find the maximum and minimum values of $f(x) = x^3 + 3xy^2 - 3x^2 - 3y^2 + 4$ [8+7]
6. (a) Find the constants a and b so that the surface $ax^2 - byz = (a + 2)x$ will be orthogonal to the surface $4x^2y + z^3 = 4$ at the point (-1,1,2).
(b) Evaluate $\oint_C (yzdx + xzdy + xydz)$ over arc of a helix $x = a \cos t, y = a \sin t, z = kt$ as t varies from 0 to 2π [8+7]
7. (a) Find $L \left[\frac{e^{-t} \sin t}{t} \right]$
(b) Solve the following differential equation using the Laplace transforms
 $\frac{d^2x}{dt^2} - 2\frac{dx}{dt} + x = e^{2t}$ with $x(0) = 2, \frac{dx}{dt} = -1$ at $t = 0$ [8+7]
8. (a) Test the convergence of the series $\frac{(n!)^2 x^{2n}}{(2n)!}$
(b) Test the convergence of the series $\sum \frac{(\sqrt{5}-1)^n}{n^2+1}$ [7+8]
